MultiRain: A GIS-based tool for multi-model estimation of regional design rainfall for scientists and practitioners

Susanna Grasso, Andrea Libertino and Pierluigi Claps

ABSTRACT

Extreme rainfall estimation is a long-standing challenge for hydrological hazard assessment and infrastructure design, particularly if considering the need to deal with climate change. Advances in statistical methods and in rainfall data availability allow for frequent updates of regional rainfall frequency analyses. These allow for new estimates that, however, cannot simply replace older ones in the risk management, due to technical, socio-economic and legislative reasons. To preserve compatibility between old and new regional estimates a multi-model approach could be used, where model uncertainties can be combined to help reach a final decision. To make this possible, one has to face the uneasy retrieval of data and results of older analyses and, quite often, non-trivial areal rainfall estimates are needed with all methods. To give an answer to these technical needs, a tool named *MultiRain* has been developed. The tool computes depth–duration–frequency (*DDF*) curves, both related to a point and integrated over an area, from multiple regional statistical analyses. The *MultiRain* procedure is based on Python scripting, GIS functions and web technologies, and can be performed via web-browser or in a desktop GIS environment. A demonstration version has been built using four different regional analyses proposed in a 20-years period for the North-West of Italy.

Key words | areal rainfall, DDF curves, design rainfall, hydrologic design tool, multi-model, regional frequency analysis

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INTRODUCTION

Risk assessment related to severe precipitation is a growing priority of hydrological practice, due to the significant consequences of these phenomena on human safety, in a context of apparent increase of the number and severity of extreme meteorological events. Most of the adverse hydrometeorological events that led to about 25,000 fatalities per year across the globe (Munich Re's NatCatService 2017) relate directly to intense rainstorms, which are difficult to forecast, both in location and in terms of expected effects, particularly in urban areas. Intensity–duration–frequency (*IDF*) or depth–duration–frequency (*DDF*) curves are commonly the starting point for design and operation of flood protection works (Grimaldi *et al.* 2011). They are mathematical relationships that allow the estimation of the average

rainfall intensity i (or the total rainfall depth h) over a given timescale d for a given return period T (e.g., Koutsoyiannis *et al.* 1998). From the *DDF* one can obtain a design hyetograph, i.e., a reference rainfall sequence to be used in rainfall–runoff modelling with various methods (e.g., Alfieri *et al.* 2008). For the evaluation of the *DDF* curves in ungauged sites, or averaged over an area, regional rainfall frequency analysis (*RFA*) is required, and many studies have been carried out to predict rainfall depths with a certain probability of occurrence in a generic location within large areas (see, e.g., Reed *et al.* 1999; Svensson & Jones 2010). The estimation is usually carried out by interpolating spatially the data or the distribution parameters estimated at the station points (e.g., Myers 1994;

Corrected Proof

2   S. Grasso *et al.* | *MultiRain*: A GIS-based multi-model design rainfall estimation tool   **Journal of Hydroinformatics | in press | 2019**

Libertino *et al.* 2018), or by pooling the data to form statistically homogeneous regions (see, e.g., Hosking & Wallis 1997).

It is not uncommon that different methods of *RFA* of extreme precipitation exist for the same regions. Quite often they adopt different techniques for identifying homogeneous regions and use different probability distributions or different methods for estimating distribution parameters. Most of the time, a new *RFA* is based on the availability of new data, even only for a limited number of years or of stations. The rationale of not totally replacing the older results with the new ones is that the hydrologic design figures used to assess the reliability of infrastructure need to be consistent over time. That is, if the design of a given infrastructure is based on estimates obtained by an 'old' study, the design of related and successive works should comply with the previous one, even though data and knowledge have increased and improved over time. At the same time, the institutions in charge of the risk management of infrastructure are very interested in the results of new methodologies, that use advanced geo-statistical techniques and data with a higher spatio-temporal resolution, to face the challenges of climate change. In fact, even if the widespread perception of an increase in the frequency of severe rainstorms does not yet find clear confirmation in the scientific literature, local correlations between the increase in temperature and the intensification of extreme rainfall are being consolidated (e.g., Westra *et al.* 2013).

To help preserve the consistency in design rainfall estimates over time, some scientific studies have promoted the simultaneous use and association of different methodological approaches over the search of a single 'best model', sometimes hard to identify (see, e.g., Shamseldin *et al.* 1997; Di Baldassarre *et al.* 2009; Velázquez *et al.* 2011; Okoli *et al.* 2018). The so-called *model-averaging* is particularly efficient when the goal is the estimation of quantiles for large return periods (Claeskens & Hjort 2008). For these high quantiles, the high estimation variance generally allows different distribution functions to be admissible after the hypothesis testing. The need to comply with this undetermined model selection assumes practical significance, for example, when considering that hydraulic safety of dams in Italy relies on the estimate of a 1,000-year flood,

and that for small basins it is very important to check that estimate using regional flood frequency analyses and rainfall–runoff methods.

The above considerations underline the usefulness of merging and harmonizing the information deriving from different methods which have evolved over time. This process, which includes the above-mentioned *model-averaging*, is called here a *multi-model* approach for the selection of the hydrologic design values. Non-trivial technical difficulties arise for the practitioners when managing this merging process, deriving from the different variables required by the methods, the different detail of reproducibility of estimates, the topographical bases used (from paper maps to GIS systems), the different probability distributions, etc.

This paper presents the technical rationale of the development of a tool that allows a fast comparison and combination of the results from different rainfall mapping studies (see, Grasso *et al.* 2018). More specifically, this tool, named *MultiRain*, is a set of GIS-based procedures designed to produce concurrent *DDF* estimates from various regional frequency analyses both at a point and over an area. To better describe the features of the *MultiRain* product, all its building phases are presented, starting with the case study of the north-west of Italy, where four existing *RFA* studies are available. The four *RFA* methodologies are first briefly summarized, along with some details required for the customization of the software tool. The *MultiRain* general features are then described, with a focus on the solutions adopted for harmonizing the presentation of the results of the four methods. An application of the *MultiRain* customized for north-west Italy is finally presented, with regard to the assessment of the rarity of a real rainfall event, where the results can be obtained with the combination of the different approaches demonstrating the tool capabilities.

DATA AND METHODS

Study area and available RF analysis

In this section, the case study will be introduced, and the available extreme rainfall mapping analyses will be described with the details needed to explain the customization required by the software tool. The case considered here refers to the

Corrected Proof

3 S. Grasso *et al.* | *MultiRain*: A GIS-based multi-model design rainfall estimation tool | **Journal of Hydroinformatics | in press | 2019**

Piemonte region, an area of about 25,000 km^2 in the north-west of Italy. Four *RFA* procedures are currently available for the area of interest, each one providing maps and procedures for the estimation of the *DDF*s for each location in the region. Automatic procedures for *DDF* computation are partly available only for one of the methods, along with some GIS support. Automatic areal rainfall estimates are not possible for all the methods. In some cases, the *RFA* parameters are provided through non-spatial tables or non-properly geo-referenced maps, that poses critical technical challenges for their systematic application.

Three of the considered methodologies are based on the index-rainfall method (Dalrymple 1960), in which the quantile of the extreme rainfall for a duration d and a return period T is obtained as:

$$h_T(d) \quad = \bar{h}(d) \cdot K_T(d) \tag{1}$$

In Equation (1), $h_T(d)$) is the design rainfall depth, $\bar{h}_d$ is the mean depth–duration curve (the index value for the duration d) and K_T is the growth function, i.e., the inverse of the non-dimensional frequency distribution, expressed as a function of T.

For the index rainfall $\bar{h}_d$ all the methods adopt the power law function:

$$\bar{h}(d) = a \cdot d^n \tag{2}$$

with a and n as coefficients estimated at-station and, in most cases, mapped by spatial interpolation.

Three *RFA*s were built using almost the same database; however, different statistical approaches are adopted, and extreme precipitation quantiles can differ considerably. A brief description of the methodologies is provided below, focusing on the characteristics that can make a direct (manual) comparison quite cumbersome.

PAI-Po design rainfall map (Po River basin)

The *PAI-Po* procedure has been developed by the Po River Authority on the 60,000 km^2 area covering the Po drainage basin, in the context of the Po River Hydrogeological Master Plan (PAI – Piano Stralcio per l'Assetto Idrogeologico, AdbPo 2001). This latter organization represents the framework behind the hydrologic and hydraulic risk assessment plan, providing rules, limitations and guidelines to be used in land and urban planning in the Po River basin.

The analysis has been carried out on 277 rain gauges, distributed over the whole basin area using the time series of the Servizio Idrografico e Mareografico Italiano (*SIMN*) of annual maxima of rainfall depth collected for the durations: 1, 3, 6, 12 and 24 hours. Data from 1929 to 1989 were considered.

The methodology is not based on the index rainfall paradigm. *DDF* curves are provided for selected return periods and are estimated by fitting the power law (Equation (2)) separately on the rainfall quantiles estimated on the data for the aforementioned durations. Therefore, independent *DDF* curves are provided for different return periods as:

$$h_T(d) \quad = a_T \cdot d^{n_T} \tag{3}$$

with a_T and n_T as the coefficients fitted by linear regression on the logarithms of the five quantiles estimated for the return period T at each station point. All quantiles are estimated using a Gumbel distribution. The return periods considered are: $T = 20$, 100, 200 and 500 years.

The a_T and n_T parameters are then interpolated on a 2 km spatial grid using ordinary kriging, to estimate *DDF* curves at ungauged locations. All the parameters in the grid covering the Po basin are provided in a table in which the location of each cell is obtained by sequential ordering of rows and columns indices. Querying individual cells on an online map is also possible (AdbPo 2001).

As this procedure does not provide results according to the index-rainfall framework, a systematic conversion has been proposed here, to make *PAI-Po* results easily comparable to the other *RFA*s. All details are provided in the Appendix.

VAPI – De Michele & Rosso RFA (NW Italy)

For the whole of north-west Italy, a study was conducted (De Michele & Rosso 2001) in the framework of a research project for the estimation of floods in Italy (VAPI project), driven by the National Group for the Prevention of Hydrogeological Disasters (CNR-GNDCI) in the 1990s. The VAPI project represents an important pillar, at national level, in hydrological risk assessment, since its main

objective was to produce methods for extreme rainfall and flood estimation at the national scale.

In this analysis (De Michele & Rosso 2001), a database of 366 stations was considered: 270 in the Po River basin and 96 in Liguria, out of the Po River basin. Station record length was at least 20 years and the average sample length was 34, ending up with a database not very different from that of the *PAI-Po* study. *DDF* curves were estimated through the index-rainfall method, using a GEV distribution (Jenkinson 1955) to represent the growth curve K_T. Parameters were estimated using the *PWM* method (Hosking *et al.* 1985). Ordinary kriging interpolation was used for mapping the parameters of Equation (2) and of the GEV at ungauged sites. The maps of *a*, *n* and of the GEV parameters (Equations (1) and (2)) for north-west Italy (including Lombardia, Piemonte, Valle d'Aosta, Liguria and Emilia-Romagna regions) were made available as images in pdf format (see Figure 1), so that the numeric information cannot be extracted.

VAPI – Villani RFA (Piemonte region)

The *VAPI Villani* RFA (Villani 2003) was later developed for the Piemonte region according to the standards suggested by CNR-GNDCI. It uses a hierarchical approach based on the two-component extreme value (TCEV) distribution (Rossi *et al.* 1984), which takes into account separately the

estimation of parameters of the ordinary and of the extra-ordinary components of the curve. The analysis was carried out on 517 rain gauges with at least ten years of observations, adding some rainfall data collected by *Regione Piemonte* and by some neighbouring French institutions during 1913–1986 to the main database of the national hydrologic service (SIMN). The spatial mapping of the TCEV parameters is obtained through a noiseless kriging (Furcolo & Villani 1998). Note that the extraordinary component of the growth curve resulted as not significant in a large proportion of the region. In that case, the TCEV collapses on a Gumbel distribution, with the higher-order parameters set as $\theta_* = 1$ and $\Lambda_* = 0$. Together with the publication of the procedure report (Villani 2003), a support software (named *Va.Pi.*) was developed, aimed at the production of *DDF* curves for single stations and for a given set of Piemonte basins. However, the limited distribution of *Va.Pi.*, which was originally developed for Windows98 and never updated afterwards, discouraged its use. The *Va.Pi.* map grids have a resolution ranging from 1 km to 5 km, depending on the variability of the represented data.

Patched Kriging RFA (Piemonte region)

The *Patched Kriging* procedure (Libertino *et al.* 2018) was undertaken to take advantage of a consistent increment in the data availability that had occurred since the previous
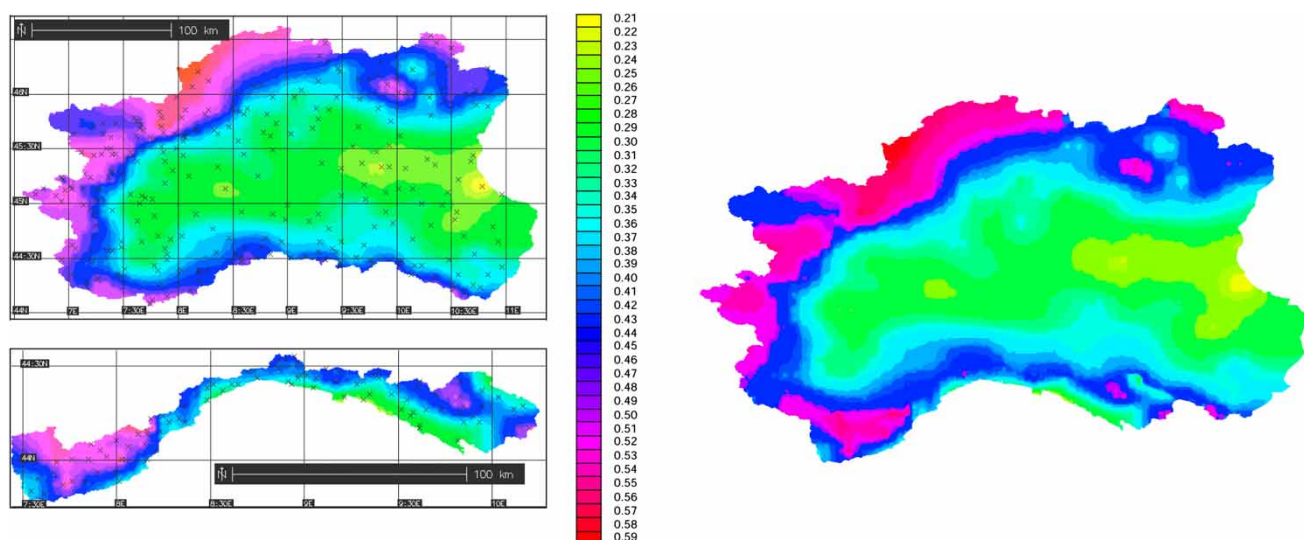

Figure 1 │ Maps of the *n* parameter of the *VAPI – De Michele & Rosso* procedure in the original paper format (left) and in the digital version (right). Please refer to the online version of this paper to see this figure in colour: http://dx.doi.org/10.2166/hydro.2019.016.

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5   S. Grasso *et al.* | *MultiRain*: A GIS-based multi-model design rainfall estimation tool   **Journal of Hydroinformatics | in press | 2019**

analyses were published. The study uses annual extreme data from 1913 to 2010, gathered from the *SIMN* and from the regional hydrologic services, for the durations 1, 3, 6, 12 and 24 hours. The methodology involves the sequential application in time of the ordinary kriging equations, producing a homogeneous dataset of synthetic series with uniform lengths. On these series, the index method is adopted and the *IDF* curves are computed according to Equations (1) and (2). The authors decided not to choose a 'best' probability distribution and to provide a map of the *a* and *n* parameters of the *DDF* and of the first three sample L-moments. This allows the end-users to choose the most appropriate probability distribution after autonomously checking of the goodness of fit. Results are provided on a 250 m gridded domain covering the areas of the Piemonte and Valle D'Aosta regions. After resampling on a 1 km grid, the results were included in a digital map embedded in a Web-GIS called *Atlante delle piogge intense in Piemonte* (ARPA Piemonte 2013) developed by the Regional Agency for Environmental Protection.

The *MultiRain* tool development

The software tool *MultiRain* described in this work operates in a geographic consistent framework, that facilitates the selection of the location of interest and the comparison of results. This is intended to allow easy comparison of results of different *RFA* methodologies and to compute the areal-averaged *DDF* curves within a basin. In the first part of this section we describe the customization problems we tackled to allow the uniform management of the existing *RFA*s in the tool. In the second part, the main approach adopted and the features that describe the possibilities of generalization for the adoption of *MultiRain* are presented. In particular, data preprocessing techniques are described, along with a brief explanation of the implementation process and of the technological details of the GIS application.

Customization issues for the Piemonte region

The main goal in the customization of the *MultiRain* tool is the building of a unique geospatial database containing all the necessary elements for the application of the different *RFA* methods available. Problems that can arise in this task derive from the heterogeneous criteria for mapping the parameters (e.g., digitized scanned images, tabulated values, ASCII raster data with different formats and resolutions) and by the methodological differences between the various regionalization approaches (e.g., the homogeneous region procedures are based on vector maps while the methods that involve the continuous spatial variation of the parameters refer to raster maps). To exemplify, some details of the customization of the four *RFA* analyses in Piemonte are provided below.

The *PAI-Po* methodology proved to be the most difficult to customize, as it provides the a_T and n_T parameters of Equation (3) on a 2 km grid, for $T = 20$, 100, 200 and 500 years. Index curve (Equation (2)) and growth curve (Equation (3)) are not provided. Starting from the knowledge that the *PAI-Po* procedure adopts a Gumbel distribution, for each cell of the gridded domain, the transformation of the results (provided as in Equation (3)) to a mapping of a and K_T parameters was accomplished by following a procedure reported in a master thesis (Magro 2007) briefly explained in the Appendix.

After the reconstruction described in the Appendix, raster maps of parameters a and n (Equation (2)), and of the two Gumbel parameters θ_1 and θ_2 have been built. The computerized procedure needed to provide the tool's functionalities, compute the *DDF* curves for whatever return period in a single cell, and is applicable to all Gumbel-based RFAs. After customization, an extensive testing was done to compare rainfall quantiles obtained from the tool with the ones available, e.g., to selected stations from the original report.

For the *VAPI – De Michele & Rosso* method, the main issue to tackle was the need to digitize the parameters' maps, which are only available in paper format and as .pdf image (see, e.g., Figure 1 (left)). For this purpose, we used an image processing procedure implemented in Matlab for extracting the colour information from the .pdf map, relating the extracted colours to the provided colour bar, and attributing a numeric value to each pixel of the image. The digital images were first noise-cleaned, i.e., unnecessary graphical elements, such as the grid lines, the station indicators, etc. were removed (see Figure 1 (left)). The numeric values derived from the Matlab procedure were then converted into raster format, suitably geo-referenced

and then merged, to connect the two separate maps provided for the Po basin and the Liguria catchments. An example of the resulting map obtained for the n coefficient is shown in Figure 1 (right).

For the *VAPI – Villani* RFA, we obtained from the *Va.Pi* software folder the raster files of parameters a and n for the mean, and of θ_*, Λ_*, Λ_1 for the TCEV growth curve. Geo-referred parameter maps were obtained converting the raster from a binary grid format (.grd) to the ASCII format (.asc) and referring the cell centroids to the WGS84/UTM Zone 32N coordinate system. In the cells where $\Lambda_* = 0$, the TCEV distribution is known to reduce to a Gumbel distribution, and this was reproduced in the *MultiRain* tool.

The maps related to the *Patched Kriging* methodology (Libertino *et al.* 2018) have been requested from the authors in raster format. Using the provided L-moments raster maps with a $250\,m \times 250\,m$ resolution, we have computed the θ_1 and θ_2 parameters of the Gumbel distribution and the θ_1, θ_2 and θ_3 parameters of the GEV, allowing evaluation of the growth curve K_T with two probability functions. This procedure has entailed minimum pre-processing customization efforts, as the raster maps of a and n were also available and already georeferenced.

MultiRain technical features

In the early stage of the *MultiRain* tool development, a Python plugin for the QGIS software (i.e., 'QGIS local plugin version') was built. In that version, the digitized regional maps, necessary to infer *DDF* curves at ungauged sites, were inserted into the plugin configuration package, to be used locally. Subsequently, with the aim to more easily distribute GIS data and functionality over the internet through standard internet protocols, specific web services have been implemented according to the OGC Web Processing Service (WPS) specification, accessible both by web browser and by using some desktop GIS programs. The use of server-side scripting allows the users to access calculations independently of the underlying software and avoid the problem of updating the plugin to keep it compatible with the updates of the various GIS programs. Moreover, data do not need to be stored locally (client-side) but are maintained by the hosting entity and can be updated and expanded on the server, without the need for the users to download updates. It should be added that computing times are usually shorter than those of the client scripting. This WPS format appeals to practitioners and planners as it reduces uncertainties and calculation errors and makes it possible to obtain *DDF* curves in an automatic way.

The connection to the WPS services is also available through a Desktop GIS software (i.e., QGIS, ArcGIS). This setting is interesting for several reasons: it allows the use of the geospatial algorithms available in the GIS software and the integration of data stored locally. Furthermore, results can be visualized directly on the map canvas enabling integration and overlay of spatial information from different sources in order to gain a deeper insight into relationships and scenario evaluation.

For sharing these procedures, a web platform has been developed, with free and open-source software, using PyWPS to set up the WPS processes, GRASS GIS as a backend to access all the geoprocessing functionalities, GisClient3 to build the WebGIS (accessible through client browsers) and Apache as web server. GisClient3 is an interesting web authoring tool configurator for PostGIS and MapServer that has the ability both to build Mapfiles and to provide OpenLayers maps. All the spatial data, necessary for *RFA*s implementation, have been registered in the GRASS database.

Despite all the pros deriving from the use of the WPS service, the use of the 'QGIS local plugin version' remains attractive, as it allows researchers to further explore rainfall frequency analysis and to carry out enlarged spatial analysis and also provides to any Python and QGIS skilled user the possibility to add other *RFA* methods.

The *MultiRain* tool, despite differences in scripting, has the same capabilities and provides the same benefits for the user in both the developed versions (the 'QGIS local plugin' and the WPS one). The user can either provide a point (as a shapefile or by inserting its coordinates) or select an area of interest (by uploading a proper shapefile). In the first case, the results are referred to the values of a pixel; in the second case, *DDF* curves of all the cells falling into the basin divide are computed and averaged spatially. Both versions of the tool allow for the following operations for all the available methodologies:

- query of all the available maps, for extraction of the parameters (point or areal);

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7   S. Grasso *et al.* │ *MultiRain*: A GIS-based multi-model design rainfall estimation tool   **Journal of Hydroinformatics** │ in press │ 2019

- computation of the index rainfall curve $\bar{h}(d)$;
- production, in a text format, of the values of the local or areal parameters of the *DDF*s curves;
- production of a graphical representation of the *DDF*s for some significant return periods.

Moreover, if the user specifies a return period *T* and a duration, the available scripts:

- compute the growth factor K_T;
- provide the design rainfall for the duration and return period requested;
- provide a graphical representation of the *DDF*s for the considered return period and duration, obtained with the different methodologies.

The WPS procedures implemented can be invoked client-side in two ways: directly from the built web-mapping application, accessible from the project website (soon available at http://www.idrologia.polito.it/MultiRainTool), or from any GIS desktop software that supports the OGC WPS standard (some software may require external plugins). In the first case, the user can either upload via web browser the polygon vector file of the area of interest or proceed, directly online, using an automatic watershed delineation service (performed using GRASS functionalities starting from a digital elevation model map, based on the NASA SRTM, designed by Ganora *et al.* (2016)). In the second case, the user can execute the WPS processes choosing the vector layer that delimitates the basin of interest from those already available into the current GIS session.

RESULTS AND DISCUSSION

The final configuration of the *MultiRain* tool customized for the Piemonte region is shown here with a series of screenshots and related comments.

Figure 2 shows an example of the execution of one of the WPS procedures from the QGIS desktop software using a WPS Client plugin. In particular, the figure
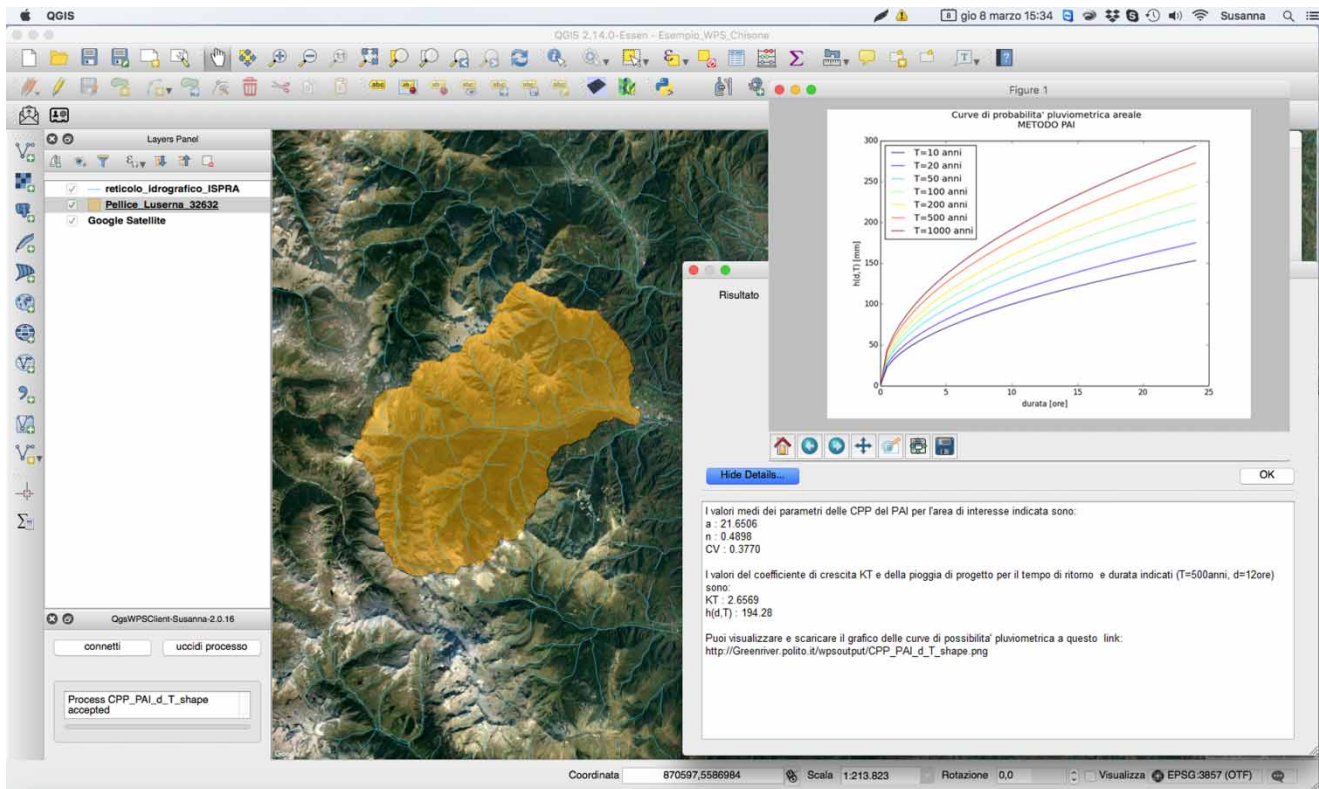

Figure 2 │ View of the results of the WPS process, served up to estimate regional depth–duration–frequency curves applying the *PAI-Po* methodology, executed from the QGIS Desktop software using a WPS plugin.

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8   S. Grasso *et al.* │ *MultiRain*: A GIS-based multi-model design rainfall estimation tool   **Journal of Hydroinformatics** │ in press │ 2019

represents the results of the application of the WPS process to estimate *DDF* curves with the *PAI-Po* methodology for a given catchment (the vector layer added into QGIS project and displayed in the map canvas) with return period $T = 500$ years and duration $d = 12$ hours. The WPS procedure provides data outputs as 'text/plain' and 'image/svg'. The values of the areal parameters of the *DDF*s and the rainfall quantile for the duration and return period requested are reported in the textbox, while a graphical representation of the *DDF*s for the considered *T* and some others significant return periods are represented in a svg format.

When the WPS process is executed directly from the web-mapping application, textual results are displayed in a webpage message box, where an URL-endpoint for retrieving the created graph is provided. In case the watershed divide is not available, it can be delimited through a WPS procedure available through the web browser, as depicted in Figure 3, starting from the definition of the outlet's coordinates.

The *MultiRain* tool QGIS plugin version allows for more in-depth analysis not only at the basin scale, but also at regional level. Indeed, the plugin provides not only the graphs or the parameters' value of the *DDF* curves for the area of interest, but also allows maps to be built of the quantiles and of the growth factors for a selected return period. This last functionality is applied to build maps of Figure 4, where the rainfall quantiles for $T = 1,000$ years and $d = 3$ hours are represented for all methods. Consistent differences among the obtained quantiles are apparent, as well visible is how the final grid resolution reflects the different spatial resolution of the original analyses.

Application example and discussion

To demonstrate the capabilities of the *MultiRain* tool, the version we have customized for NW Italy is applied with regard to the assessment of rarity of a real rainfall event, where the results that can be obtained with the different approaches demonstrate a typical experience from the practitioner viewpoint.

The example concerns the Pellice River, a basin with an area of about 216 km^2, which was affected by significant flooding in November 2016 (ARPA Piemonte 2016) generated by a strong and persistent precipitation event. The chosen reference rainfall station is Luserna San Giovanni (361006, 4963859 in the reference system WGS84 – UTM
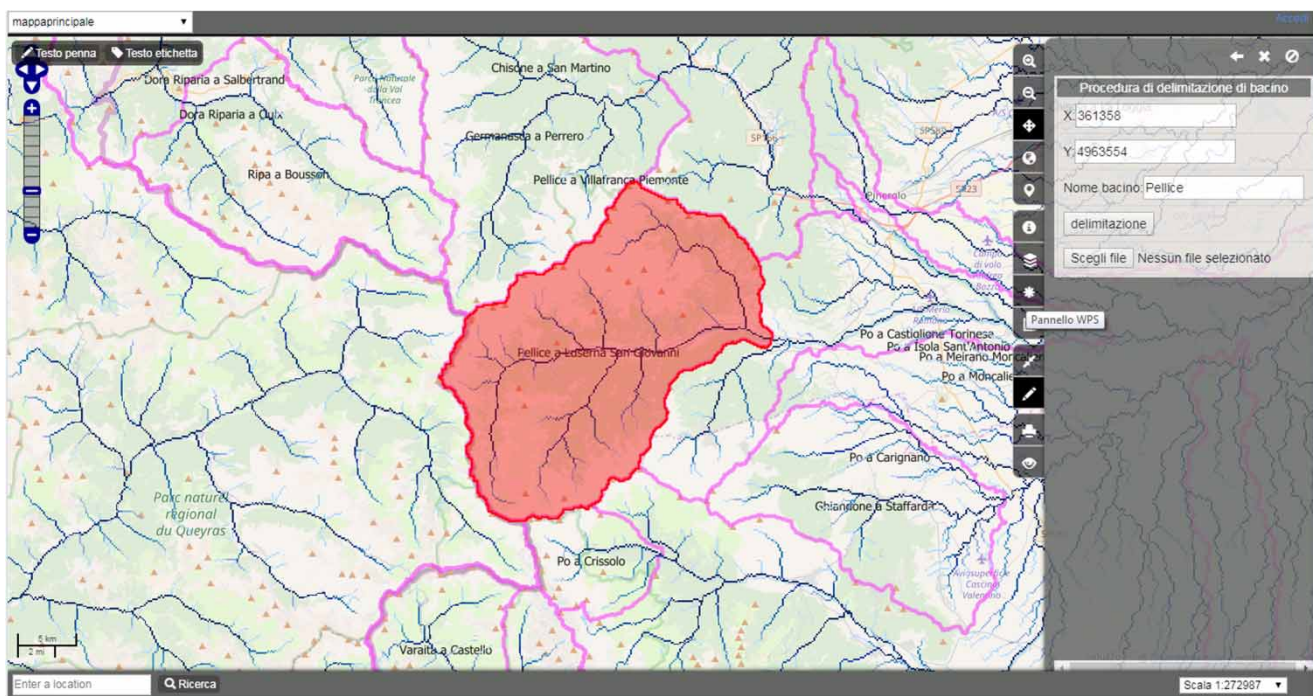

Figure 3 │ Screenshot representing the interface of *MultiRain* tool on the Web browser (the Pellice River basin is highlighted).
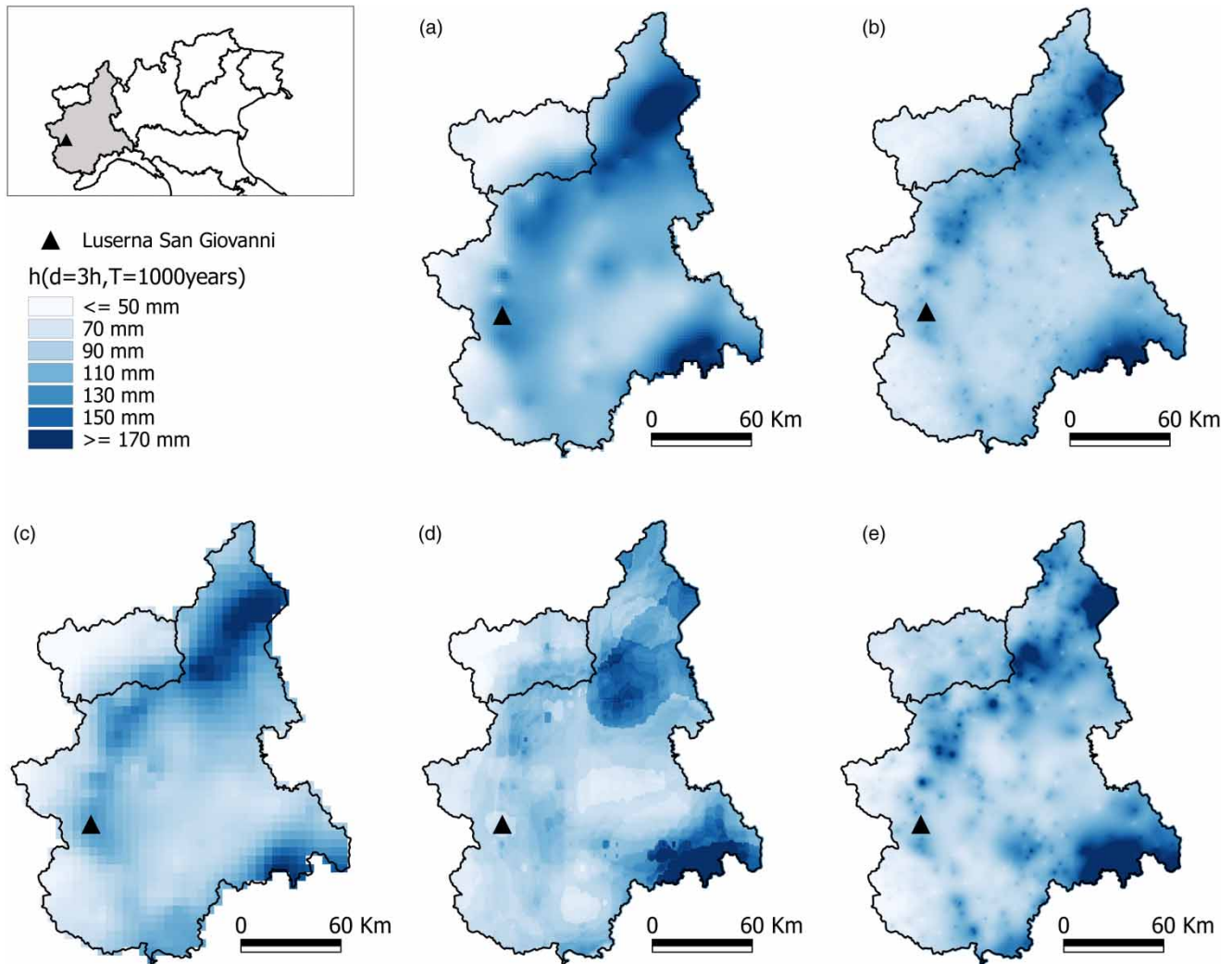
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9   S. Grasso *et al.* │ *MultiRain*: A GIS-based multi-model design rainfall estimation tool   **Journal of Hydroinformatics** │ in press │ 2019

Figure 4 │ Comparison of design rainfall depth maps for *T* = 1,000 years and *d* = 3 hours, obtained for the methods: (a) *PAI-Po*, (b) *Patched Kriging* using Gumbel distribution, (c) *VAPI Villani*, (d) *VAPI De Michele & Rosso*, (e) *Patched Kriging* using GEV distribution.

32N), positioned at the outlet of the basin (see black triangle in the maps of Figure 4). The *MultiRain* tool has been applied to estimate the return period of the rainfall event, through the four described methods.

Five different families of *DDF* curves are obtained, since the *Patched Kriging* model can estimate quantiles with both the Gumbel and the GEV distributions. The curves obtained with *T* = 500 are represented in Figure 5 both at the station location (left) and averaged at the basin scale (right). Comparing local and areal curves, one can notice that the spatial average reduces the differences that emerge on site estimation.

In order to estimate the return period of the November 2016 event, the maximum rainfall depths for 1, 3, 6, 12 and 24 hour durations, recorded during the storm were considered (see Table 1, column 2) and compared with the *DDF* curves of the different *RFA*s, exploiting the potentialities of *MultiRain*. The return periods for a 24 hour duration is estimated by all methods between 200 and 500 years, with the exception of the *VAPI – De Michele & Rosso* method, that suggests a return period of over 5,000 years. Figure 6 (left) shows the graph where this assessment is made using the most recent and data-rich method (the *Patched Kriging*) using a Gumbel distribution.
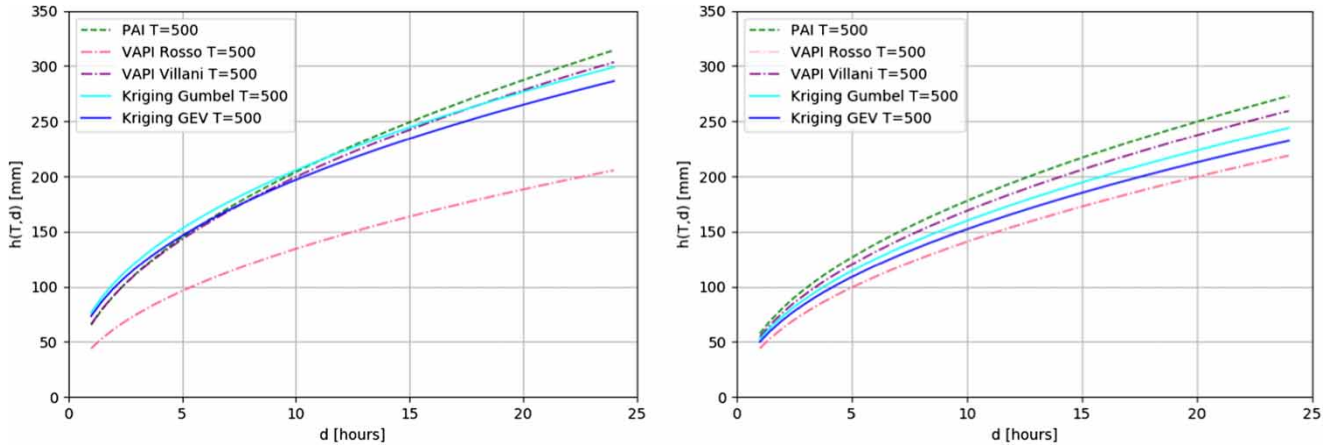
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10   S. Grasso *et al.* │ *MultiRain*: A GIS-based multi-model design rainfall estimation tool   Journal of Hydroinformatics │ in press │ 2019

Figure 5 │ (Left) *DDF* curves for *T* = 500 years for the Luserna San Giovanni station and (right) areal *DDF* curves for *T* = 500 years for the Pellice basin at Luserna San Giovanni.

Table 1 │ Estimated return periods using all the available *RFA*s for the observed extreme precipitation event at Luserna San Giovanni rainfall gauge

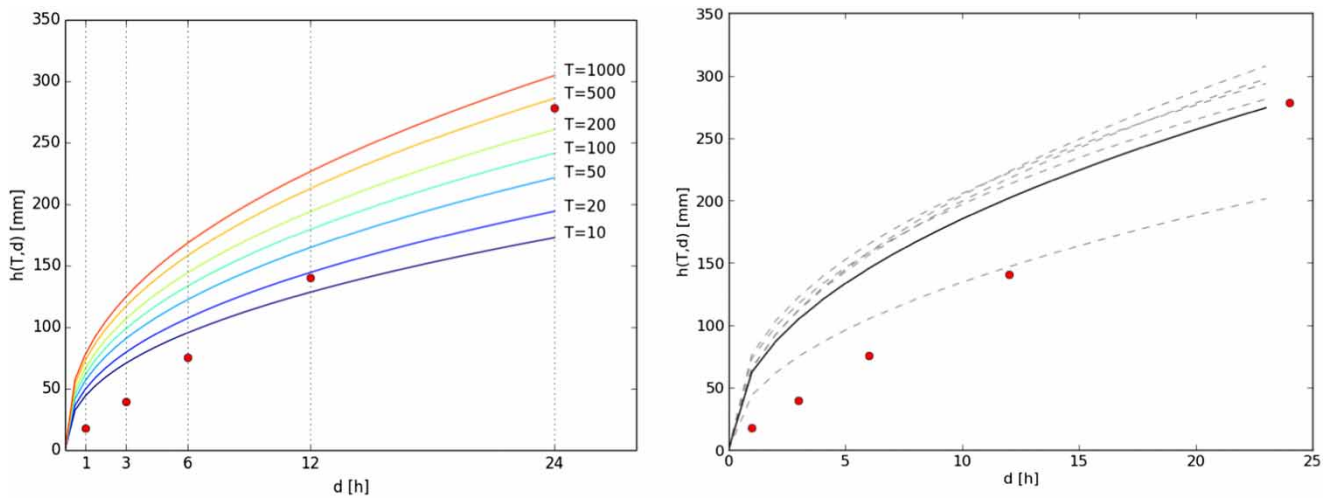| Duration (h)	Cumulated rainfall depth (mm)	Return time *T* (years) for different models				
		PAI	***VAPI Villani***	***VAPI Rosso***	***Patched Kriging* Gumbel**	***Patched Kriging* GEV**
1	17.6	1.20	1.37	1.31	1.06	1.06
3	39.4	1.81	2.17	2.16	1.42	1.42
6	75.6	4.55	5.74	8.95	3.53	3.48
12	140.6	17.00	22.31	210.01	16.14	16.87
24	278.6	175.84	242.23	>5,000	263.27	375.89

Figure 6 │ Comparison of the event-maxima recorded in Luserna San Giovanni in November 2016 with (left) the *DDF* curves estimated with the *Patched Kriging* and with (right) the model-averaged *DDF* curve for *T* = 500 years (in bold) as compared to the individual *T* = 500.

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11   S. Grasso *et al.* | *MultiRain*: A GIS-based multi-model design rainfall estimation tool   **Journal of Hydroinformatics** | in press | 2019

To provide wider understanding of what can happen in similar situations, when various methods provide significantly different results and it is not possible to identify a 'best' model, the *MultiRain* tool helps in adopting a *model-averaging* approach, commonly considered a robust way to manage parameters and model uncertainty in quantile estimation.

In detail, for a certain return period, the averages of the a, n and $K(T)$ among the available methodologies can be computed to obtain an averaged curve. Differential weight can be given to the different estimates in the averaging phase, according to the expertise of the user. As a demonstration of the model-averaged result, the $T = 500$ averaged curve is computed, giving equal weight to the considered *RFA*s, and shown in Figure 6 (right) together with the 2016 event dots. The result of the overlapping of the data with the curve shows that a robust estimation of the return period for the 24 hour duration is closer to $T = 500$ than to $T = 200$ or to $T = 5,000$ years.

CONCLUSIONS

When hydrologic design values encounter updates of the estimation procedures, information deriving from different sets of data and of regional statistical estimation procedures needs to be harmonized or merged. In other conditions, e.g., for critical infrastructures, when a 'best model' is difficult to identify, the *multi-model* approach allows for the consideration of a wide range of scenarios and the adoption of robust estimates in the design and control phases.

In this framework, the *MultiRain* tool presented here aims at providing a fast operational aid to apply a *multi-model* approach to the regional rainfall frequency estimation. The tool offers estimates of depth–duration–frequency curves both for a generic location in the region considered, and as a spatial average. The estimate and comparison of spatial averages is given when the user uploads a shapefile of the contour of the area of interest (usually a watershed divide). The *MultiRain* Web Processing Services implemented, accessible both by web-browser and by Desktop GIS software, allows the user to carry out a thorough comparative analysis based on the results derived from different methodologies, without installing software and downloading data.

Despite the web platform being developed in a modular and reproducible way to allow future integrations, the need for maintaining appropriate control on the security of the data, of the scripts and of the Web server itself has led us to keep the online platform closed to editing. All the extensions and editing of the *MultiRain* WPS Service must be performed by the authors. Skilled users, interested in expanding the potentialities of the tools, can take advantage of the free availability of the 'QGIS local plugin version', that allows the source code to be edited and the integration of further data and methodologies.

Future developments will be addressed first and foremost at integrating the tool with procedures for improving its customization, needed for its implementation in further regions.

Tool availability

Final refinements to the user-interface of the web services are in development and the *MultiRain* tool web page will be available soon at: wwww.idrologia.polito.it/MultiRainTool.

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12   S. Grasso *et al.* | *MultiRain*: A GIS-based multi-model design rainfall estimation tool   Journal of Hydroinformatics | in press | 2019

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